

9.85

9.85 A Piper Cub airplane has a gross weight of 1750 lb, a cruising speed of 115 mph, and a wing area of 179 ft<sup>2</sup>. Determine the lift coefficient of this airplane for these conditions.

For equilibrium  $\mathcal{L} = W = 1750 \text{ lb}$ , where  $\mathcal{L} = C_L \frac{1}{2} \rho U^2 A$   
 Thus, with  $U = (115 \text{ mph}) \frac{(88 \frac{\text{ft}}{\text{s}})}{(60 \text{ mph})} = 169 \frac{\text{ft}}{\text{s}}$

$$C_L = \frac{\mathcal{L}}{\frac{1}{2} \rho U^2 A} = \frac{1750 \text{ lb}}{\frac{1}{2} (0.00238 \frac{\text{slugs}}{\text{ft}^3}) (169 \frac{\text{ft}}{\text{s}})^2 (179 \text{ ft}^2)} = \underline{\underline{0.288}}$$

9.86

9.86 A light aircraft with a wing area of 200 ft<sup>2</sup> and a weight of 2000 lb has a lift coefficient of 0.40 and a drag coefficient of 0.05. Determine the power required to maintain level flight.

For equilibrium  $\mathcal{L} = W = 2000 \text{ lb} = C_L \frac{1}{2} \rho U^2 A$

$$\text{or } 2000 \text{ lb} = (0.40) \frac{1}{2} (0.00238 \frac{\text{slugs}}{\text{ft}^3}) U^2 (200 \text{ ft}^2)$$

Hence,

$$U = 145 \frac{\text{ft}}{\text{s}}$$

Also,  $\mathcal{P} = \text{power} = \mathcal{D} U$ , where

$$\mathcal{D} = C_D \frac{1}{2} \rho U^2 A = (0.05) \frac{1}{2} (0.00238 \frac{\text{slugs}}{\text{ft}^3}) (145 \frac{\text{ft}}{\text{s}})^2 (200 \text{ ft}^2) = 250 \text{ lb}$$

Note: This value of  $\mathcal{D}$  could be obtained from

$$\frac{W}{\mathcal{D}} = \frac{\mathcal{L}}{\mathcal{D}} = \frac{C_L}{C_D} = \frac{0.40}{0.05} = 8, \text{ or } \mathcal{D} = \frac{W}{8} = \frac{2000 \text{ lb}}{8} = 250 \text{ lb}$$

Thus,

$$\mathcal{P} = 250 \text{ lb} (145 \frac{\text{ft}}{\text{s}}) = 3.63 \times 10^4 \frac{\text{ft} \cdot \text{lb}}{\text{s}} \left( \frac{1 \text{ hp}}{550 \frac{\text{ft} \cdot \text{lb}}{\text{s}}} \right) = \underline{\underline{65.9 \text{ hp}}}$$